Person Fit Analysis for Assessing Academic Writing Performance Using Rasch Model

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Journal info	
Glasser Education Journal	Abstract.
p-ISSN: 2579-5082	Assessing academic writing performance is a critical aspect
e-ISSN: 2598-2818	of educational practices. The thesis is derived from writing is
DOI: <u>10.32529/glasser.v7i2.2571</u>	an essential skill that students need to develop to succeed
Volumes: 7	academically and professionally. To fulfill this, the Rasch
Number: 2	model offers important test statistics that play a crucial role
Month: 2023	in constructing tests related to evaluation and item selection problems, as well as in decision-making regarding the
Keywords: Person Fit, Writing Assessment, Rasch Model	generated test scores. Building upon this narrative, this research is conducted with the aim of identifying person fit in assessing academic writing performance using the Rasch model. The sample in the form of essays was obtained from a group of 40 students who had previously undergone a six- month academic writing program. The data was then analyzed using Ministep 4.8.2.0 built for Rasch Model analysis. The analysis results indicated that there were 31 students in the person misfit category, suggesting a need to reconsider the appropriateness of the conducted treatment

model's profile.

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A. INTRODUCTION

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academic Assessing writing performance is a critical aspect of educational practices. The thesis is derived from writing is an essential skill that students need to develop to succeed academically and professionally. То do that academic writing should demonstrate knowledge, present arguments, and communicate ideas effectively. Therefore, it is important to evaluate students' writing skills accurately and reliably to assess whether those qualities have been accommodated properly and adequately in students' essays.

Traditional assessment methods, such as rubrics and checklists, may not provide the rigor required for reliable assessments (Fisher, 2007; Wibisono, 2018). These methods rely on subjective judgments by evaluators, which can lead to inconsistent and unreliable results. As a result, many researchers have explored statistical methods writing to assess performance objectively and reliably (Bond & Fox, 2007; Boone & Yale, 2014). It is a statistical method that has been widely used in educational research to evaluate various constructs, including academic writing performance (Engelhard, 1992; Fisher, 2007; 301

and whether there were other factors contributing to it. Additionally, a discrepancy was found in 5 students with persons misfit or overfit, and their better performance was observed on more difficult items, contrary to the Rasch Razak & Thien, 2012). It also provides an objective and reliable method for evaluating writing performance. It allows for the analysis of item and participant responses to evaluate writing skills accurately.

In recent years, there has been a growing interest in the application of the Rasch Model to assess person fit in academic writing performance. Several studies have investigated the use of this model to evaluate writing skills and identify students who may require additional support or challenge to improve their performance. A recent study by Osman et al (2012) examined the use of the Rasch Model to assess person fit into a group of Chinese graduate students' academic writing performance. The study found that the Rasch Model provided a reliable and valid means of assessing writing skills and identifying students who required additional support. Another study by Li et al (2021) investigated the use of the Rasch Model to assess the writing skills of Chinese undergraduate students. The study found that person fit analysis using the Rasch Model could accurately identify students who were performing below their expected ability level and who required additional support to improve their writing skills. A study by Rahman (2023) examined the application of the Rasch Model to assess person fit and item fit in a group of Indonesian students' academic writing performance in blended learning program. The study found that person fit analysis using the Rasch Model could accurately identify students who were

performing above their expected ability level and who required more challenging writing tasks to further develop their writing skills.

Despite the Rasch Model's usefulness in evaluating writing performance, limited research has explored its application in assessing person fit in academic writing assessment. Person fit refers to the degree to which an individual's responses fit with the Rasch Model. Identifying person fit issues is crucial as it can help identify students who have either cheated during the test or have lower or higher abilities than the Rasch Model estimated. Detecting person fit issues and taking appropriate actions can improve the accuracy and reliability of the assessment results.

In the context of academic writing performance, person fit analysis is essential as it can help educators and researchers identify students who require additional support to improve their writing skills. It can also help identify students who may be performing above their estimated ability, and thus, require more challenging writing tasks. Furthermore, person fit analysis can provide insights into the effectiveness of educational interventions aimed at improving students' writing skills. By identifying students with person fit issues, educators and researchers can monitor the effectiveness of educational interventions and make necessary adjustments to improve students' writing performance.

Therefore, this study aims to explore the application of the Rasch Model to analyze person fit in assessing academic writing performance. The study's findings can contribute to the development of more objective and reliable methods for assessing academic writing performance. Moreover, the results can inform educational practices and the development of more effective interventions to support students' academic writing performance.

This study's significance lies in its potential to improve the accuracy and reliability of the assessment results. By analyzing person fit, educators and researchers can identify students who require additional support to improve their writing skills, which can enhance their academic and professional success. Additionally, the study's results can contribute to the development of more effective educational interventions to improve students' writing skills.

In conclusion, person fit analysis using the Rasch Model can provide insights into students' academic writing performance and inform educational practices to support their learning. The study's results can contribute to the development of more reliable and objective methods for assessing writing performance, leading to more effective interventions to improve students' writing skills.

B. RESEARCH METHODS

This study involved 40 EFL students from Eloquensi English Language Centre who had completed the TOEFL iBT essay writing course. They possessed an intermediate or advanced level of English proficiency. The main task assigned to them was to compose essays consisting of five paragraphs. The essays followed a standardized format with an introduction, content, and conclusion. The intention behind implementing this standardized structure was to guarantee impartial evaluations by the assessors, as the essay's paragraph count could potentially impact the rating, positively or negatively.

The Rasch model is employed in this study for analysis purposes due to its ability to capture the interaction between respondents and items simultaneously. In contrast to raw scores, the Rasch model employs logit values to express the probability of an item being chosen by a group of participants (Sumintono, B. & Widhiarso, 2013; Tan, 2013). The purpose of using the Rasch model is to estimate the expected raw score for Likert ratings, which are ordinal in nature and do not have equal intervals between scores. Andrich (1978) expanded the application of the Rasch model to polytomous data by incorporating two core principles: the measurement of individual ability or agreement level and the measurement of item difficulty in achieving agreement (Misbach & Sumintono, 2014). For data analysis purposes, the output utilized includes summary statistics (Figure 1) to gather reliability information. Additionally, the output includes unidimensionality items (Figure 2) and Fit Order items (Figure 3) for assessing validity.

This study employed a holistic rubric developed by Jacob et al (Jacobs et al, 1981) as the measurement tool. The rubric consists of six levels of measurement, namely proficient, fluent, expanding, developing, beginning, and emerging. The criteria column reveals that the assessment focuses on four key elements of writing ability: content, structure, diction, and mechanics. Content encompasses the introduction, ideas or body paragraphs, and the logical organization of thoughts. Structure evaluates not only grammatical proficiency within sentences but also the composition of paragraphs using different sentence types (simple, compound, complex, and compoundcomplex). Diction assesses the respondent's vocabulary usage and word variations within a paragraph to avoid word repetition. Lastly, writing mechanics examines the correct implementation of punctuation, spelling, and capitalization.

Rating		Criteria
		es single or multiple paragraphs with clear introduction, fully develop idea,
	-	ent idea logically
		appropriate verb tense and a variety of grammatical and syntactical structures;
Proficient		complex sentences effectively; uses smooth transitions
		varied, precise vocabulary
	4. Has o	occasional errors in mechanics (spelling, punctuation, and capitalization) which do
	not d	letract from meaning
	1. Writ	es single or multiple paragraphs with main idea and supporting detail, present idea
	logic	ally, though some parts may not fully develop
Fluent	2. Uses	appropriate verb tense and a variety of grammatical and syntactical structures;
Fluent	error	s in sentence do not detract from meaning; uses transitions
	3. Uses	varied vocabulary appropriate for the purpose
	4. Has t	few errors in mechanics which do not detract from meaning
	1. Orgar	nizes ideas in logical or sequential order with some supporting detail; begins to
	write	a paragraph
	2. Exper	iment with a variety of verb tenses, but does not use them consistently;
Expanding	subje	ct/verb agreement errors; uses some compound and complex sentences; limited
	use of	f transitions
	3. Vocal	bulary is appropriate to purpose but sometimes awkward
		punctuation, capitalization, and mostly conventional spelling; errors sometimes
		ere with meaning
		s sentences around an idea; some sequencing present, but may lack of cohesion
	2. Write	in present tense and simple sentences; has difficulty with subject/verb agreement,
	run-o	n sentences are common; begin to use compound sentences
Developing	3. Uses	high frequency words; may have difficulty with word order; omit endings or
	words	-
		some capitalization, punctuation and transitional spelling; errors often interfere
		meaning
		to convey meaning through writing
Beginning		predominantly phrases and patterned or simple sentences
Deginning		limited or repetitious vocabulary
		temporary (phonetic) spelling
		vidence of idea development or organization
Emerging		single word, pictures, and patterned phases
Linei Sing		es from model
	4. Little	awareness of spelling, capitalization, or punctuation

 Table 1. Jacob et al Holistic Rubric (1981)

The six measurement levels mentioned earlier are converted into five Likert ratings, as shown in table 2. It is necessary to interpret the values into a Likert scale in order to facilitate the further processing of the raw scores using ministep software.

Table 2.	Rubin	Kating Scale	
Scale	1	Likert Score	
Proficient		5	
Fluent		4	
Expanding		3	
Developing		2	
Emerging	&	1	
Beginning			

Table 2 Rubric Rating Scale

Based on the necessary analysis, there are eight steps for analyzing person fit using the Rasch model.

- Collect data on academic writing ability assessments. This data can be in the form of a scale or numerical values given by assessors for each item on the academic writing ability test.
- 2. Prepare the data in the appropriate format for Rasch analysis. The data must be in matrix form, with rows representing participants and columns representing test items.
- Run the Rasch analysis on the data using statistical analysis software that allows for Rasch analysis. The results of the analysis will include calculations of participant ability values and item difficulty levels.
- 4. Conduct person fit analysis by examining participants' standard residuals. Standard residuals are the difference between the estimated ability of participants and their observed ability. High standard residuals indicate that participants have values that do not fit the Rasch model, indicating cheating in test answers.
- Identify participants with high standard residuals and review their test answer results. It is possible that some items do not

fit the participant's ability, or the participant may have cheated in answering the test.

- Re-evaluate test items and participant values. Identify and eliminate test items that do not fit the Rasch model and/or participants who cheated in answering the test.
- Perform a Rasch model analysis again on the updated data to check for improvements in person fit and suitability of data to the Rasch model.
- 8. Interpret the results of the Rasch and person fit analysis. These results can be used to inform practices in evaluating academic writing ability and improving the quality of academic writing ability tests and measurements.

C. RESULTS AND DISCUSSION

Three sets of output data are utilized to assess the validity and reliability of individuals and items in student essays. The initial set of output data comprises summary statistics. The second set involves item statistics, which aids in identifying items that do not fit well. Lastly, person statistics are examined to identify individuals who do not fit well. The data outputs for this study were obtained through the application of the Rasch model analysis using ministep software. This particular software is specifically designed for statistical analysis related to Rasch modeling 03-299WS SUMMARY STATISTICS - Notepad

SUMM	ARY OF 40	MEASURED	PERSON					
	TOTAL			MODEL	IN	FIT	OUTF	IT
	SCORE		MEASURE		-		-	
MEAN	14.2		.04					
SEM	.4	.0	1.10	.46	.12	.18	.13	.16
P.SD	2.7	.0	6.87	2.90	.76	1.10	.79	1.02
S.SD	2.7	.0	6.96	2.93	.77	1.11	.80	1.04
MAX.	19.0	4.0	12.27	7.63	3.47	2.93	3.06	2.08
MIN.	10.0	4.0	-9.09	1.08	.00	-1.36	.00	-1.38
REAL RM	SE 4.36	TRUE SD	5.31 SEP	ARATION	1.22 PER	SON REL	IABILITY	.60
	SE 4.33	TRUE SD	5 33 SEP.	ARATTON	1.23 PER	SON REL	ΤΑΒΤΙ ΤΤΥ	.60

FIGURE 1. Summary Statistics

In this section, the summarized research findings are presented, as shown in Figure 1. Figure 1 displays the outfit MNSQ (outliersensitive or information-weighted fit Mean Square) statistics used to identify whether individuals fit or misfit the Rasch model, along with their accompanying characteristics. Figure 1 presents a summary of statistics. The person measure is 0.04, indicating the average value of respondents' performance in the essay writing assessment. An average value higher than 0.0 logit suggests that respondents tend to meet the standards outlined in the rubric. Cronbach's alpha value is utilized to assess the overall reliability of the interaction between individuals and items. The summary statistics reveal a Cronbach's alpha value of 0.92, indicating a high level of reliability. Person reliability demonstrates the consistency of measurements, indicating that repeated measurements will yield similar information. In other words, if another party were to conduct the same measurement, the values obtained would not differ significantly. Minor differences may still exist, which are considered acceptable. However, if significant differences arise in the results of the same sample analyzed by different researchers, several factors should be examined, including temporal similarity (stability), equivalence of assessment instruments, internal consistency of elements within the instrument, and agreement among raters. In Figure 1, the person reliability value is 0.60.

INPUT: 4	40 PERSON	4 ITEM	REPORTED	: 40 PERSO	N 4 ITEM	4 CATS	MINISTEP 4.8.2.0
PERSON:	REAL SEP.	.: 1.22	REL.: .60	ITEM:	REAL SEP.	: 1.46	REL.: .68

PERSON STATISTICS: MISFIT ORDER

ENTRY	TOTAL											MATCH	
NUMBER	SCORE	COUNT	MEASURE	S.E.	MNSQ	ZSTD		ZSTD		EXP.		EXP%	PERSO
27	13	4	-3.21	1.18	3.47	2.93			A .33		25.0	74.2	527
35	19	4	12.27								50.0	76.7	\$35
40	18	4	10.97	1.08	1.94	2.14	2.18	2.08	C68	.38	25.0	65.4	540
30	14	4	-1.99	1.08	1.94	2.05	2.16	2.02	D68	.38	25.0	65.5	\$30
20	14	4	-1.99	1.08	1.57	1.39	1.75	1.46	E27	.38	25.0	65.5	S20
18	11	4	-7.81	1.23	1.53	.89	1.45	.74	F16	.39	50.0	76.4	S18
24	11	4	-7.81	1.23	1.53	.89	1.45	.74	G16	.39	50.0	76.4	S24
10	17	4	9.73	1.21	1.15	.45	.99	.32	H .16	.28	75.0	75.1	S10
37	13	4	-3.21	1.18	1.11	.38	.96	.27	I .16	.29	75.0	74.2	\$37
1	14	4	-1.99	1.08	.73	66	.67	65	J .68	.38	75.0	65.5	S1
21	10	4	-9.09	1.08	.73	67	.67	65	K .68	.38	75.0	65.4	S21
22	10	4	-9.09	1.08							75.0		
26	14	4	-1.99								75.0		
6	13	4	-3.21	1.18					N .63		75.0		
5	19	4	12.27								100.0		
7	19	4	12.27	1.25	.46	82	.36	70	P.94	.39	100.0	76.7	S7
15	19	4	12.27						Q .94		100.0		
16	11	4	-7.81						R .94		100.0	76.4	S16
19	11	4	-7.81						S .94		100.0		
23	11	4	-7.81	1.23					T .94		100.0		
25	11	4	-7.81	1.23					t .94		100.0		
28	11	4	-7.81								100.0		
2	12	4	-5.45	1.87					r .00		100.0		
3	12	4	-5.45								100.0		
4	12	4	-5.45	1.87					p.00		100.0		
13	12	4	-5.45								100.0		
17	12	4	-5.45						n .00		100.0		
29	12	4	-5.45								100.0		
8	16	4	4.59						1.00		100.0		
9	16	4	4.59								100.0		
11	16	4	4.59						j.00		100.0		
12	16	4	4.59								100.0		
14	16	4	4.59						h .00		100.0		
31	16	4	4,59						g .00		100.0		
32	16	4	4.59						f .00		100.0		
33	16	4	4.59						e .00		100.0		
34	16	4	4.59	7.63							100.0		
36	16	4	4.59								100.0		
38	16	4		7.63									
39	16	4	4.59	7.63	.00	-1.36	.00	-1.38	a .00	.05	100.0	99.6	\$39
MEAN	14.2	4.0	.04	3.22	. 59	5	.57	5			84.4	83.7	
P.SD	2.7	.0									24.8		

FIGURE 2. Person Statistics: Misfit Order

According to Linacre (2002), there are two statistics that can be used to assess the fit of data to the Rasch model, namely infit (inliersensitive or information-weighted fit) and outfit (outlier-sensitive or information-weighted fit). These statistics are commonly reported in the form of (MNSQ) mean squares and standardized z-values (ZSTD). **MNSO** represents the average of squared residuals for an item, while ZSTD (standardized form) is a transformation of the average squared values with sample size correction (Bond & Fox, 2015). Therefore, in this study, to determine whether an item or respondent (person) fits or misfits the Rasch model, the output of the Winsteps Rasch software, specifically the Outfit Mean Square (MNSQ) statistics, needs to

be interpreted. MNSQ statistics are chosen because they are independent of sample size.

Students	Outfit MNSO	Students	Outfit MNSO
27	3.06	4	0.4
45	2.64	13	0.4
40	2.18	17	0.4
30	2.16	29	0.4
20	1.75	8	0.0
5	0.36	9	0.0
7	0.36	11	0.0
15	0.36	12	0.0
16	0.34	14	0.0
19	0.34	31	0.0
23	0.34	32	0.0
25	0.34	33	0.0
28	0.34	34	0.0
2	0.4	36	0.0
3	0.4	38	0.0
39	0.0		
Li	nacre (2002) r	provides a	rule of thur

Table 3. Person Misfit Summarv

Linacre (2002) provides a rule of thumb to assess the implications of model fit on measurement. An MNSQ value greater than 2.0 indicates a damaging effect on the measurement system, while a value between 1.5 and 2.0 suggests a lack of meaning in the measurement. MNSQ values between 0.5 and 1.5 are considered beneficial for measurement, and an MNSQ value below 0.5 is not useful for measurement but does not disrupt the measurement system. Figure 2 presents a summary of difficulty levels and outfit MNSQ statistics. According to Linacre's criteria (2002), person fit statistics are interpreted. The results show that 31 out of 41 students are classified as person misfits, namely students with identification numbers 27, 35, 40, 30, 20, 15, 16, 19, 23, 25, 28, 2, 3, 39, 4, 13, 17, 29, 8, 9, 11, 12, 14, 31, 32, 33, 34, 36, and 38. This means that the abilities of these 31 students have response patterns that cannot be predicted by the model (Smith, 2001). However, response patterns can depict the accuracy of each student's response to each item (Sumintono & Widhiarso, 2015). One way to identify the causes of person misfit is through Guttman matrices or scalograms. Guttman matrices provide valuable information as the items have been ordered from the easiest item, mechanic (4), to diction (3), structure (2), and content (1). These matrices can also indicate the unidimensionality of the data (Hambleton & Swaminathan, 1991). Below is the scalogram of the 40 students based on the identification of difficulty levels from lowest to highest. Identification of students classified as person misfits based on the Guttman matrices.

TABLE 2	22.1 DA		INISTEP.	xlsx		Z0U29	9WS.TXT	April 31 2023 11:	5
INPUT:	40 PER	SON	4 ITEM	REPORTED:	40 PERSON	4 ITEM	4 CATS	MINISTEP 4.8.2.0	
		GRAM	OF RESP	DNSES:					
PERSON									
	4132								
-		~							
	+5554								
	+5554								
	+5554								
	+4555								
	+4545								
	+4344								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4444								
	+4433								
	+4334								
	+4343								
	+3434								
6	+4333	S6							
27	+4243	527							
37	+3433	\$37							
2	+3333	S2							
3	+3333	\$3							
4	+3333	54							
13	+3333	S13							
17	+3333	517							
	+3333								
	+3332								
	+3233								
	+3332								
	+3332								
	+3323								
	+3332								
	+3332								
	+3232								
22	+3232	522							
	4132								

FIGURE 3. Guttman Scalogram of Responses

Based on the presentation of the Guttman matrix above, it can be concluded that students with the identification numbers 35, 40, 10, 30, and 37 are considered person misfits in the Rasch model. This is because these students exhibit unusual response patterns, achieving high scores on more difficult items such as content and structure (Jacobs et al, 1981), but obtaining low scores on easier items like diction and mechanics. According to the definition of the Rasch model, which states that students with lower abilities should not have a high likelihood of correctly answering more challenging items, it can be inferred that there may have been an error in assessing the students' writing skills.

This identification result aligns with Meijer (1996) and Karabatsos (2003), who mention at least five possible causes of person misfit. These include cheating (such as copying answers from other test-takers), where unfair behaviour leads to correct answers on items that the student couldn't have answered correctly; careless responding, which occurs when test-takers answer difficult items correctly but answer easy items incorrectly in an unclear manner; lucky guessing, when testtakers randomly guess the correct answer on items they don't actually know; creative responding, which only occurs among highability test-takers who respond incorrectly to easy items because they interpret the items in a 309

unique and creative way; and finally, random responding, which refers to situations where test-takers randomly choose multiple-choice options when responding to items. Furthermore, the Rasch model identified three students with identification numbers 5, 57, and 15 as individuals who did not fit well within the model. This determination was made due to their extreme scores, which led to unmeasurable fit statistics, indicating an overfit. According to Meijer (1996), measuring person fit not only identifies impossible response patterns but also patterns that are too likely. The Rasch model predicts uncertainty, and having too much certainty actually indicates limitations in responses.

D. CLOSING

Based on the analysis results using the Outfit MNSQ range, it was found that there were 31 students who were classified as person misfit. This indicates that there is a discrepancy in the understanding and application of the 4 skills in academic writing taught to the students. As a result, these 31 students are unable to effectively apply the sub-parameters or items (Jacob et al) of the academic four parameters in writing. Additionally, anomalies were found in the students' response patterns to more difficult items such as content writing and correct structure application. Both of these items received significantly higher scores compared to the other two items, mechanics and diction, which are relatively easier for the students to master. There are 5 students who fall into this misfit category, as shown in the scale map by better scores on the more difficult items

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